



Fourth Semester B.E. Degree Examination, Feb./Mar. 2022

Additional Mathematics - II

Time: 3 hrs.

Max. Marks: 80

Note: Answer FIVE full questions, choosing ONE full question from each module.

Module-1

- 1 a. Find the rank of the matrix :

$$A = \begin{bmatrix} 0 & 1 & -3 & -1 \\ 1 & 0 & 1 & 1 \\ 3 & 1 & 0 & 2 \\ 1 & 1 & -2 & 0 \end{bmatrix}$$

(06 Marks)

- b. Show that the following system of equations is inconsistent.

$$\begin{aligned} 2x - 3y + 7z &= 5 \\ 3x + y + 3z &= 13 \\ 2x + 19y - 47z &= 32. \end{aligned}$$

(05 Marks)

- c. If the eigen values of the matrix $\begin{bmatrix} 1 & 1 & 3 \\ 1 & 5 & 1 \\ 3 & 1 & 1 \end{bmatrix}$ are $-2, 3, 6$ find the eigenvectors corresponding to each of the eigenvalue.

(05 Marks)

OR

- 2 a. Computer the eigenvalues of the matrix

$$\begin{bmatrix} 3 & 1 & 4 \\ 0 & 2 & 6 \\ 0 & 0 & 5 \end{bmatrix}$$

(06 Marks)

- b. Solve by Gauss elimination method :

$$\begin{aligned} x + y + z &= 9 \\ 2x - 3y + 4z &= 13 \\ 3x + 4y + 5z &= 40. \end{aligned}$$

(05 Marks)

- c. Compute inverse of a matrix $\begin{bmatrix} 1 & 4 \\ 2 & 3 \end{bmatrix}$ applying Cayley – Hamilton theorem.

(05 Marks)

Module-2

- 3 a. Solve $(D^2 - 5D + 6)y = 0.$

(06 Marks)

b. Solve $\frac{d^2y}{dx^2} + 8y = \sin(3x).$

(05 Marks)

- c. Solve by the method of undetermined coefficients the differential equation :

$$\frac{d^2y}{dx^2} + \frac{2dy}{dx} + 4y = 2x^2 + 3e^{-x}.$$

(05 Marks)

OR

- 4 a. Solve $\frac{d^2y}{dx^2} - \frac{3dy}{dx} + 2y = e^{4x}$. (06 Marks)
- b. Solve $\frac{d^2y}{dx^2} - \frac{4dy}{dx} + 4y = e^{2x} \cos x$. (05 Marks)
- c. Solve by the method of variation of parameters, $\frac{d^2y}{dx^2} + 4y = \tan(2x)$. (05 Marks)

Module-3

- 5 a. Find Laplace transform of $f(t) = 6 + e^{3t} + \sin(4t) + \cos(6t) + t^4$. (06 Marks)
- b. Find $L\left\{\int_0^t \sin(4t) dt\right\}$ applying Laplace transforms of integrals rule. (05 Marks)
- c. If $f(t) = \begin{cases} t^2 & 0 < t < 2 \\ t & t > 2 \end{cases}$
Express $f(t)$ in terms of unit step function and hence find the Laplace transform. (05 Marks)

OR

- 6 a. Find L.T. of :
 i) $\sin(5t) \cos(2t)$ ii) $\cos^2(3t)$. (06 Marks)
- b. Apply rule of transforms derivatives to find $L\{f'(t)\}$ for $f(t) = \cos t$ where $f'(t) \equiv$ derivative of $f(t)$. (05 Marks)
- c. Find the Laplace transform of the periodic function :

$$f(t) = E \sin(\omega t) \quad 0 < t < \frac{\pi}{\omega}$$

$$= 0 \quad \frac{\pi}{\omega} < t < \frac{2\pi}{\omega}$$
 (05 Marks)

Module-4

- 7 a. Find inverse Laplace transform :

$$\frac{1}{s^{\frac{3}{2}}} - \frac{2s}{s^2 + 64} + \frac{10}{s^2 - 100} + \frac{1}{s+8} + \frac{1}{s}$$
 (06 Marks)
- b. Find :
 $L^{-1}\{\bar{f}(s)\}$ if $\bar{f}(s) = \frac{1}{s(s-1)(s-2)}$. (05 Marks)
- c. Solve using Laplace transforms :

$$\frac{dx}{dt} + 5x - 2y = t$$

$$\frac{dy}{dt} + 2x + y = 0$$

Given $x = 0, y = 0$ at $t = 0$.

(05 Marks)

OR

- 8 a. Find :

$$L^{-1} \left\{ \frac{3s+4}{s^2 + 2s + 2} \right\}.$$

(06 Marks)

b. Find : $L^{-1} \left\{ \log \sqrt{\frac{s+3}{s+4}} \right\}.$

(05 Marks)

- c. Apply Laplace transform method to solve

$$y''' + 2y'' - y' - 2y = 0$$

$$\text{given } y(0) = y'(0) = 0$$

$$\text{and } y''(0) = 6.$$

(05 Marks)

Module-5

- 9 a. Explain the terms:

i) Probability

ii) Sample space

iii) Mutually exclusive events with an example.

(06 Marks)

- b. If three coins are thrown find the probability that,

All the three are heads

Atleast one tail occurs.

(05 Marks)

- c. If $P(A) = \frac{1}{4}$ $P(B) = \frac{1}{3}$ $P(A \cap B) = \frac{1}{12}$ find the conditional probabilities,

i) $P(A|B)$

ii) $P(B|A)$.

(05 Marks)

OR

- 10 a. For any, two events A and B state the 'law of addition' of probabilities. Also for two independent events A and B state the 'law of multiplication' of probabilities. (06 Marks)

- b. If three persons hit a target with probabilities $P(A) = \frac{1}{2}$ $P(B) = \frac{1}{3}$ $P(C) = \frac{1}{4}$. Find the probability that, i) All hit the target ii) Target not hit. (05 Marks)

- c. In a bolt factory three machines A, B, C produce 20%, 30% and 50% of the total output and of their outputs 5%, 4%, 3% are defective respectively. If a bolt is chosen randomly and found defective, find the probability that bolt was manufactured by machine A. (05 Marks)

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